MOODY'S MEGA MATH CHALLENGE 2007

RISKY BUSINESS: USING MATHEMATICAL MODELING TO MAXIMIZE RETURNS AND MINIMIZE RISK IN THE STOCK MARKET

TEAM #104

SUMMARY

The goal of any investor, whether the commodity is a stock, bond, or other security, is to maximize earning potential while limiting risk. In attempting to reach an equilibrium between these two factors, we utilized several mathematical models based on various data.

Using the given data on the Free Cash Flow, Return on Invested Capital (ROIC), Price to Earnings ratio, Price to Sales ratio, and Beta coefficient, we created two portfolios that resulted in relatively high gains with relatively low risk. However, these gains would not have been sufficient to entice any but the most frivolous investors, so we created a system to maximize potential returns while minimizing risk.

Using concepts such as professional analysis, Sharpe Ratios, and historical figures in conjunction with the given data, we were able to create the best possible portfolio from the eighteen given stocks. By directly comparing a stock's potential ROIC to its standard deviation (a derivative of its Beta coefficient), we were able to construct a portfolio that is expected to return a high profit while putting relatively little capital at risk.

Assumptions Made

The stock market will steadily increase: given in the problem.

No more than \$30,000 can be invested: given in the problem.

Each portfolio created contains exactly **six** stocks: the problem sets the maximum at six, and it would be unwise to select less than six because portfolio diversification allows for both greater profitability and greater security.

Any one stock's value, and therefore the entire portfolio's value, has an equal chance of increasing as decreasing: it would be unreasonable to expect complete security in the stock market. While the market as a whole will increase, individual securities fluctuate on a day-to-day and year-to-year basis.

There will be no significant inflation over the next year: the inflationary increase that normally occurs over the course of one year would not affect the market in a large enough way so as to change the eventual outcome of this exercise.

Stock Picks and Amounts Invested

Upon first examining the data provided in the table, we decided that two of the stronger indicators of a stock's profitability are the health of its company and the value of the stock versus its price. The first is measured by the Free Cash Flow; the second is measured by the Price to Sales (P/S) ratio. In order to find the stocks that are most profitable according to these guidelines, we organized the list of stocks into two lists: the first in order of Cash Flow from highest to lowest, and the second in order of P/S ratio from lowest to highest.

Table 1a		
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Stock	Cash Flow	
CAI	3.92	
COGN	2.03	
MFE	2.02	
BMC	1.58	
SRX	1.50	
ADBE	1.38	
CTXS	1.37	
SPSS	1.24	
MSFT	1.20	
SYMC	1.20	
CDNS	1.10	
ADVS	0.87	
RHT	0.85	
ORCL	0.83	
INFY	0.78	
QADI	0.47	
NUAN	0.40	
MSCS	0.10	

	Table 1b		
A١	verage P/S	Ratio:5.0	19
	Stock	P/S	
	CAI	0.79	
	SRX	1.14	
	QADI	1.18	
	MSCS	2.17	
	SPSS	2.80	
	SYMC	3.22	
	COGN	3.72	
	BMC	4.08	
	CDNS	4.21	
	MFE	4.94	
	NUAN	5.35	
	CTXS	5.49	
	ORCL	5.52	
	ADVS	5.88	
	MSFT	6.06	
	ADBE	9.33	
	INFY	10.92	
	RHT	13.54	

We found that five stocks were ranked above average on both scales: CAI, COGN, MFE, BMC, and SRX. Our sixth stock choice, SPSS, ranked well above average on the P/S ratio scale and only three cents below the average Cash Flow. After making these choices, we also came to the realization that the Beta coefficients of the six stocks are distributed in a very even manner. One could be considered a low-risk investment (SRX), one a high-risk investment (MFE), and four moderate-risk investments (BMC, CAI, COGN, and SPSS).

When dividing the \$30,000, we first decided which stocks would receive the most money. Our first conclusion was that, since it has the lowest Beta coefficient by far and therefore has the potential to make the least money over the course of a single year, SRX would receive the least money. We decided on an arbitrary value of \$2,500 to invest in this stock. In order to make the most money possible, we decided to invest the most money in the high-risk, high-integrity stock MFE. We assumed that, in the worst-case scenario, the high-risk stock would lose enough money to offset average profits from two of the moderate stocks. With that in mind, we used the following equation to determine the amount invested in MFE:

30,000 - 2,500 = 27,500 = 4x + y = 6x,

where x is equal to the amount invested in a moderate stock and y is equal to the amount invested in MFE. This calculation resulted in an investment of \$9,166 in MFE. After these two investments, a sum of \$18,332 remained to be invested. We divided this amount evenly between the four moderate stocks, allotting \$4,583 for each.

After dividing these theoretical totals by the share prices and multiplying the resulting number of shares by the price per share, our portfolio resulted in the following:

Stock Symbol	Theoretical Total Invested	Price per Share	Shares Purchased	Total Invested	% of Portfolio's Total Value
BMC	\$4,583.00	\$29.96	152	\$4,553.92	15.19%
CAI	\$4,583.00	\$46.41	98	\$4,548.18	15.17%
COGN	\$4,583.00	\$39.78	118	\$4,694.04	15.66%
MFE	\$9,166.00	\$29.98	305	\$9,143.90	30.50%
SPSS	\$4,583.00	\$33.50	136	\$4,556.00	15.20%
SRX	\$2,500.00	\$23.69	105	\$2,487.40	8.30%

Table 2

The total value of the portfolio is \$29,983.44, leaving \$16.56 that cannot be invested.

Using More Data

After calculating our portfolio's expected rate of return and its overall risk, we came to the realization that a strong portfolio cannot be based solely on these two parameters. We repeated the above process of selecting six stocks, this time using the Return on Invested Capital (ROIC) value and the Price to Earnings (P/E) ratio in addition to the P/S and Cash Flow values. We again organized the eighteen stocks in order from most favorable to least favorable, shown below.

Cash Flow	P/S	ROIC	P/E
CAI	CAI	INFY	ORCL
COGN	SRX	MSFT	CAI
MFE	QADI	BMC	CDNS
BMC	MSCS	ORCL	MSFT
SRX	SPSS	QADI	QADI
ADBE	SYMC	CTXS	SYMC
CTXS	COGN	COGN	COGN
SPSS	BMC	SRX	SRX
MSFT	CDNS	MFE	BMC
SYMC	MFE	ADBE	CTXS
CDNS	NUAN	SPSS	MFE
ADVS	CTXS	CAI	MSCS
RHT	ORCL	CDNS	SPSS
ORCL	ADVS	RHT	ADBE
INFY	MSFT	ADVS	NUAN
QADI	ADBE	SYMC	INFY
NUAN	INFY	MSCS	RHT
MSCS	RHT	NUAN	ADVS

Table 3

BMC and COGN, two of our original picks, ranked above average on all four scales. QADI and CTXS ranked above average on three scales, so we chose them as well. For our final two picks, we chose ORCL and MSFT. These stocks ranked above average on two scales and only slightly below average on the other two. We classified two of these new choices (CTXS and QADI) as high-risk and the other four as moderate-risk.

In dividing the \$30,000 among the stocks in this new portfolio, we repeated the assumption that the worst realistic loss inflicted by a high-risk stock can be compensated for by the profits of two moderate stocks. We designated the two stocks featured in both portfolios

(BMC and COGN) as the compensators, and so allotted twice as much to those as to the high-risk stocks. For the sake of simplicity, the other two moderate stocks (MSFT and ORCL) received the same amounts as the high-risk stocks. The allotments in the second portfolio can therefore be modeled by the following equation:

$$30,000 = 4x + 2y = 8x,$$

where x is equal to the amount invested in each high-risk stock and y is equal to the amount invested in each compensating moderate stock. The amount invested in each high-risk stock is therefore 3,750 and the amount invested in each compensator is twice that, or 7,500. Again, some small changes occurred after actually purchasing the stocks, and our second portfolio resulted in the following:

Stock Symbol	Theoretical Total Invested	Price per Share	Shares Purchased	Total Invested	% of Portfolio's Total Value
BMC	\$7,500.00	\$29.96	251	\$7,519.96	25.07%
COGN	\$7,500.00	\$39.78	188	\$7,478.64	24.93%
CTXS	\$3,750.00	\$31.26	120	\$3,751.20	12.51%
MSFT	\$3,750.00	\$27.76	135	\$3,747.60	12.49%
ORCL	\$3,750.00	\$16.71	224	\$3,743.04	12.48%
QADI	\$3,750.00	\$8.07	465	\$3,752.55	12.51%

Table 4

The total value of this portfolio is \$29,992.99, leaving a sum of \$7.01 uninvested.

						EXPECTED			
	2002-2003	2003-2004	2004-2005	2005-2006	2006-2007	RETURN	VARIAN	STD DEV	Sharpe Ratio
SYMC	-4.93%	18.17%	-53.93%	-21.10%	0.42%	-12.27%	5.91%	24.31%	-0.7154
MSFT	-59.86%	2.97%	-3.05%	12.58%	2.02%	-9.07%	6.70%	25.89%	-0.5479
SRX	29.00%	30.10%	-12.43%	-7.33%	-100.00%	-12.13%	22.44%	47.37%	-0.3642
MSCS	-66.30%	13.68%	26.33%	79.25%	-59.55%	-1.32%	30.19%	54.94%	-0.1172
CDNS	-55.77%	47.40%	1.42%	23.68%	6.27%	4.60%	11.71%	34.22%	-0.0152
ADBE	-23.48%	27.47%	70.92%	-47.97%	10.62%	7.51%	16.93%	41.15%	0.0581
ORCL	-15.31%	10.70%	4.00%	9.70%	22.06%	6.23%	1.50%	12.26%	0.0904
ADVS	-79.45%	53.62%	-2.68%	56.33%	22.73%	10.11%	24.74%	49.74%	0.1003
MFE	-42.93%	30.34%	25.33%	7.85%	23.22%	8.76%	7.25%	26.92%	0.1353
CAI	-4.98%	28.90%	28.44%	19.05%	-29.41%	8.40%	5.09%	22.56%	0.1453
COGN	-17.23%	36.71%	34.42%	-6.83%	2.26%	9.87%	4.79%	21.88%	0.2169
BMC	-22.42%	29.56%	-23.27%	44.40%	38.32%	13.32%	8.94%	29.90%	0.2741
QADI	-4.55%	187.85%	-37.68%	-9.55%	7.89%	28.79%	65.48%	80.92%	0.2925
CTXS	-23.84%	64.29%	10.18%	59.11%	-17.52%	18.44%	13.81%	37.16%	0.3585
SPSS	-35.46%	62.54%	-5.49%	82.06%	5.81%	21.89%	19.14%	43.75%	0.3834
NUAN	-23.60%	23.33%	-32.97%	217.47%	18.29%	40.50%	83.23%	91.23%	0.3879
RHT	-4.74%	324.49%	-52.67%	156.46%	-21.34%	80.44%	201.35%	141.90%	0.5308
INFY	-6.34%	33.22%	33.22%	33.22%	33.22%	25.31%	2.50%	15.82%	1.2760

Table 5

Choosing the Perfect Portfolio

As a means of improving our stock choices and increasing the success of our portfolio, we used the Sharpe Ratio to add another element to consider in making our decisions. The Sharpe Ratio can be defined with the equation

$$S = \frac{E[R - R_f]}{\sigma}$$

where the Risk Free Rate of return is subtracted from the asset return and then divided by the standard deviation. The Sharpe Ratio represents the ratio between high return and low risk.

INFY	1.2670
RHT	0.5308
NUAN	0.3879
SPSS	0.3834
CTXS	0.3585
SYMC	-0.7154
QADI	0.2925
BMC	0.2741
COGN	0.2169
CAI	0.1453
MFE	0.1353
ORCL	0.0904
ADBE	0.0581
CDNS	-0.0152
MSCS	-0.1172
SRX	-0.3642
MSFT	-0.5479
SYMC	-0.7154

Table of Sharpe Ratios

First Trial

To begin choosing our best portfolio we chose the 6 companies that had the greatest Sharpe Ratio. These were SPSS, RHT, CTXS, INFY, NUAN, and QADI. We added their Sharpe Ratios (SR) together creating a total sum (TS):

 $SR_{SPSS} + SR_{RHT} + SR_{CTXS} + SR_{INFY} + SR_{NUAN} + SR_{QADI} = TS$ (0.3834) +(0.5308) + (0.3585) + (1.2670) + (0.3879) + (0.2925) = 3.2291

We then divided each Sharpe Ratio by the total sum to determine the percentage of our \$30,000 budget that would go into each stock.

$$\begin{split} & \text{SPSS} = 0.3834/3.2291 = .1187100\% &= 11.87\% \\ & \text{RHT} = 0.5308/3.2291 = .1644 \text{ X } 100\% &= 16.44\% \\ & \text{CTXS} = 0.3585/3.2291 = .1110 \text{ X } 100\% &= 11.10\% \\ & \text{INFY} = 1.2670/3.2291 = .3952 \text{ X } 100\% &= 39.52\% \\ & \text{NUAN} = 0.3879/3.2291 = .1201 \text{ X } 100\% &= 12.01\% \\ & \text{QADI} = 0.2925/3.2291 = .0906 \text{ X } 100\% &= 9.06\% \\ &= 100\% \end{split}$$

After calculating this, we multiplied each percentage by \$30,000 to determine the amount of money we would invest in each particular company.

= 11 87%	times $\$30000 = \3561
= 16.44%	times $\$30.000 = \4.932
= 11.10%	times $\$30,000 = \$3,330$
= 39.52%	times $30,000 = 11,856$
= 12.01%	times $30,000 = 3,603$
= 9.06%	times $30,000 = 2,718$
	Sum of Investments (SOI) = $30,000$

This, however, led to a variance of 23.19%, a standard deviation of 48.15%, and a return value of 32.74%. This generated an expected profit of \$9,821.08. So although the revenue from the investments would be a good amount of money, the risk and high standard deviation percentage led us to change investments in different stocks.

Second Trial

We then looked to replacing the companies with the largest Sharpe Ratio since we thought this was driving up our standard deviation. We first decided to remove RHT due to its low return and overpricing (according to the P/E, investors would pay \$61.38 for every \$1 of earnings) and replace it with BMC. We utilized our same process:

 $SR_{SPSS} + SR_{BMC} + SR_{CTXS} + SR_{INFY} + SR_{NUAN} + SR_{QADI} = TS$ (0.3834) +(0.2741) + (0.3585) + (1.2670) + (0.3879) + (0.2925) = 2.9724
$$\begin{split} & \text{SPSS} = 0.3834/2.9724 = .1290 \text{ X } 100\% &= 12.90\% \\ & \text{BMC} = 0.2741/2.9724 = .0922 \text{ X } 100\% &= 9.22\% \\ & \text{CTXS} = 0.3585/2.9724 = .1206 \text{ X } 100\% &= 12.06\% \\ & \text{INFY} = 1.2670/2.9724 = .4293 \text{ X } 100\% &= 42.93\% \\ & \text{NUAN} = 0.3879/2.9724 = .1305 \text{ X } 100\% &= 13.05\% \\ & \text{QADI} = 0.2925/2.9724 = .0984 \text{ X } 100\% &= 9.84\% \end{split}$$

Multiply by \$30,000 to determine the amount invested in each:

= 12.90%	times \$30,000 = \$3,870
= 9.22%	times \$30,000 = \$2,766
= 12.06%	times \$30,000 = \$3,618
= 42.93%	times \$30,000 = \$12,879
= 13.05%	times \$30,000 = \$3,915
= 9.84%	times \$30,000 = \$2,952
	SOI = \$30,000

This, however, resulted in a variance of 10.15%, a standard deviation of 31.86%, and a return of 22.43%, with an expected profit of \$6,728.03.

Third Trial

We now tried to rotate BMC with INFY and bring back RHT into our portfolio:

 $SR_{SPSS} + SR_{RHT} + SR_{CTXS} + SR_{BMC} + SR_{NUAN} + SR_{QADI} = TS$ (0.3834) + (0.5308) + (0.3585) + (.2741) + (0.3879) + (0.094) = 2.2272

We calculate the percentage of each SR in the total SR of the portfolio:

$$\begin{split} & \text{SPSS} = 0.3834/2.2272 = .1721\ 100\% &= 17.21\% \\ & \text{RHT} = 0.5308/2.2272 = .2383\ X\ 100\% &= 23.83\% \\ & \text{CTXS} = 0.3585/2.2272 = .1610\ X\ 100\% &= 16.10\% \\ & \text{BMC} = .2741/2.2272 = .1231\ X\ 100\% &= 12.31\% \\ & \text{NUAN} = 0.3879/2.2272 = .1742\ X\ 100\% &= 17.42\% \\ & \text{QADI} = 0.094/2.2272 = .1313\ X\ 100\% &= 13.13\% \end{split}$$

Multiply by \$30,000 to determine the amount of money invested in each:

SPSS = 17.21%	times \$30,000 = \$5,163
RHT = 23.83%	times $30,000 = 7,149$
CTXS = 16.10%	times \$30,000 = \$4,830
BMC = 12.31%	times \$30,000 = \$3,693
NUAN = 17.42%	times \$30,000 = \$5,226
QADI = 13.13% t	times \$30,000 = \$3,939
	SOI = \$30,000

This resulted in a variance of 34.31%, a standard deviation of 58.58%, a return of 34.60%, and a profit of \$10,380. Since both cases where we replaced the higher value with BMC resulted in a standard deviation higher than our return we discarded this idea and decided to keep INFY due to its low standard deviation and its high return but completely eliminate RHT from further combinations of stocks for our portfolio because of its constant increase in standard deviation and because it is overpriced (as mentioned earlier).

Fourth Trial

We then picked a new combination without RHT and QADI due to their extremely high standard deviations 141.90% and 80.92% respectively.

 $SR_{BMC} + SR_{ORCL} + SR_{CAI} + SR_{COGN} + SR_{INFY} + SR_{CTXS} = TS$ (0.2741) + (0.0904) + (0.1453) +(0.2169) (1.2760) + (0.3585) = 2.3612

We calculate the percent of each SR in the total SR of the portfolio:

BMC = 0.2741/2.3612 = .1161 X 100% = 11.61%ORCL = 0.0904/2.3612 = .0383 X 100% = 3.83%CAI = 0.1453/2.3612 = .0615 X 100% = 6.15%COGN = 0.2169/2.3612 = .0919 X 100% = 9.19%INFY = 1.2760/2.3612 = .5404 X 100% = 54.04%CTXS = 0.3585/2.3612 = .1518 X 100% = 15.18%

Multiply by \$30,000 to determine the amount invested in each:

BMC = 11.61%	times \$30,000 = \$3,483
ORCL = 3.83%	times $30,000 = 1,149$
CAI = 6.15%	times \$30,000 = \$1,845
COGN = 9.19%	times \$30,000 = \$2,757
INFY = 54.04%	times \$30,000 = \$16,212
CTXS= 15.18%	times \$30,000 = \$4,554
	SOI = \$30,000

This resulted in a significant drop in the variance 1.75%, a standard deviation of 13.22%, and a return of 16.88%, with an expected gross profit of \$5,065.31.

Fifth Trial

In our final analysis of the Sharpe Ratios and trial-and-error method we came up with a lineup of stocks that would yield us maximum profit along with a standard deviation that would be lower than our return.

 $SR_{BMC} + SR_{CAI} + SR_{COGN} + SR_{INFY} + SR_{MFE} + SR_{ORCL} = TS$ (0.2741) + (0.1453) + (0.2169) + (1.2760) + (0.1353) + (0.0904) = 2.138

We calculate the percent of each SR in the total SR of the portfolio:

 $BMC = 0.2741/2.138 = .1282\ 100\% = 12.82\%$ $CAI = 0.1453/2.138 = .0633\ X\ 100\% = 6.33\%$ $COGN = 0.2169/2.138 = .0680\ X\ 100\% = 6.80\%$ $INFY = 1.2670/2.138 = .1014\ X\ 100\% = 10.14\%$ $MFE = 0.1353/2.138 = .5968\ X\ 100\% = 59.68\%$ $ORCL = 0.0904/2.138 = .0423\ X\ 100\% = 4.23\%$

We then multiply again by \$30,000:

BMC = 12.82%	times \$30,000 = \$3,846
CAI = 6.33%	times \$30,000 = \$1,899
COGN = 6.80%	times \$30,000 = \$2,040
INFY = 10.14%	times \$30,000 = \$3,042
MFE = 59.68%	times \$30,000 = \$17,904
ORCL = 4.23%	times \$30,000 = \$1,269
	SOI = \$30,000

This combination resulted in our variance of 2.56%, a standard deviation of 16.01%, a return of 18.94%, and an expected profit of \$5,681.17. We now had a positive difference of 2.93 between the return and the standard deviation, making this our best possible choice.

Table 6

	BMC	CAI	COGN	INFY	MFE	ORCL		
% of Portfolio	12.82%	6.80%	10.14%	59.68%	6.33%	4.23%		100.00%
Expected Return	13.32%	8.40%	9.87%	25.31%	8.76%	6.23%		
	Hi	storical F	Returns					
	вмс	CAI	COGN	INFY	MFE	ORCL		
March 02 - March 03	-22.42%	-4.98%	-17.23%	-6.34%	-42.93%	-15.31%		
March 03 - March 04	29.56%	28.90%	36.71%	33.22%	30.34%	10.70%		
March 04 - March 05	-23.27%	28.44%	34.42%	33.22%	25.33%	4.00%		
March 05 - March 06	44.40%	19.05%	-6.83%	33.22%	7.85%	9.70%		
March 06 - March 07	38.32%	-29.41%	2.26%	33.22%	23.22%	22.06%		
	вмс	CAI	COGN	INFY	MFE	ORCL		
BMC	8.94%	-1.07%	-0.41%	2.83%	3.85%	2.85%		
CAI	-1.07%	5.09%	3.03%	1.06%	1.82%	-0.45%		
COGN	-0.41%	3.03%	4.79%	2.14%	4.58%	0.94%		
INFY	2.83%	1.06%	2.14%	2.50%	4.09%	1.70%		
MFE	3.85%	1.82%	4.58%	4.09%	7.25%	2.80%		
ORCL	2.85%	-0.45%	0.94%	1.70%	2.80%	1.50%		
Variance x %Porfolio	0.36%	0.13%	0.29%	1.51%	0.27%	0.07%	Variance Standard	2.56%
							Deviation	16.01%
Return for each stock	1.71%	0.57%	1.00%	15.10%	0.55%	0.26%	Return	18.94%
							Expected	
							Gross Profit	\$5,681.17
Individual Variance	2.83%	1.58%	2.51%	2.39%	4.06%	1.56%		

 $16.83\% \quad 12.56\% \quad 15.85\% \quad 15.45\% \quad 20.16\% \quad 12.48\%$

Conclusion:

Ind Std. Dev



Assuming that our chance to get a profit or loss are the same and knowing our expected return minus 1 standard deviation is 2.93%, the interval (-1, infinity) of standard deviation would have an 84% chance of getting a 2.93% or more profit. This is why we have partially secured a profit of 2.93% or more with the combination of these investments.

Other Justifications

After finding the "perfect" portfolio using Sharpe Ratios, we used several methods to verify our results. The first of these took the form of professional analysis from Internet sources. Shown below are the buying recommendations of one such source. On a scale of one to five, with one meaning "strongly buy" and five meaning "strongly sell," Yahoo.com recommends the following:

Stock Name	Yahoo.com's Recommendation
ADBE	2
ADVS	2
BMC	3.1
CAI	2.8
CDNS	2
COGN	2.5
CTXS	2.2
INFY	1.8
MFE	2.3
MSCS	2.5
MSFT	2
NUAN	1.6
ORCL	2.2
QADI	2.3
RHT	2.6
SPSS	2.2
SRX	2.7
SYMC	2.8

Table 7

All six of the stocks selected for the final portfolio have ratings of "hold" or better, and one even has a rating between "buy" and "strongly buy." Interestingly enough, there are several options that come more highly recommended by the analysts; needless to say, there are certainly more elements that factor into a stock's success than the purely mathematical ones. The disparity between the advice and our portfolio can be explained by our lack of knowledge in the non-mathematical areas of the stock market game.

In addition to these analyses, we also compared our six stocks to the S&P 500 and the Dow Jones Industrial Average over the space of five years. The dark blue lines represent the returns on the six stocks, and the teal lines represent the average values of the indices. BMC, CAI, COGN, and INFY consistently rank higher than the indices. MFE and ORCL, while usually below the indices, rise at the same pace as the indices and can therefore be considered safe and profitable investments.







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